# Ch 10.3: Convolutional Neural Nets

Lecture 31 - CMSE 381

Prof. Mengsen Zhang

Michigan State University

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Dept of Computational Mathematics, Science & Engineering

Fri, April 11, 2025

#### Announcements

#### Last time:

- Multilayer NN
- pyTorch

#### This lecture:

CNNs

#### Final countdown:

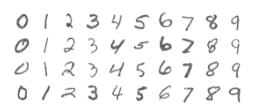
- HW #9 is due Sunday 4/13
- Exam 3 is 4/21
- Project is due 4/25

	M	3/17	Midterm #2		Sun 3/16
21	W	3/19	Polynomial & Step Functions	7.1-7.2	
22	F	3/21	Step Functions; Basis functions; Start Splines	7.2-7.4	
23	M	3/24	Regression Splines	7.4	
24	W	3/26	Decision Trees	8.1	HW #6 Due Wed 3/26
25	F	3/28	Random Forests	8.2.1, 8.2.2	HW #7 Due
26	M	3/31	Maximal Margin Classifier	9.1	Sun 3/30
27	W	4/2	SVC	9.2	
28	F	4/4	SVM	9.3, 9.4	HW #8 Due
29	M	4/7	Single Layer NN	10.1	Sun 4/6
30	W	4/9	Multi Layer NN	10.2	
31	F	4/11	CNN	10.3	HW #9 Due
32	М	4/14	Unsupervised learning / clustering	12.1, 12.4	Sun 4/13
33	W	4/16	Virtual: Project Office Hours		
	F	4/18	Review		
	M	4/21	Midterm #3		
	W	4/23			
	F	4/25			Project Due

### Section 1

Last time: Neural Nets

### **MNIST**



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- Goal: Build a model to classify images into their correct digit class
- Each image has  $p = 28 \cdot 28 = 784$  pixels
- Each pixel is grayscale value in [0,255]
- Data converted into column order
- Output represented by one-hot vector  $Y = (Y_0, Y_1, \dots, Y_9)$
- 60K training images, 10K test images

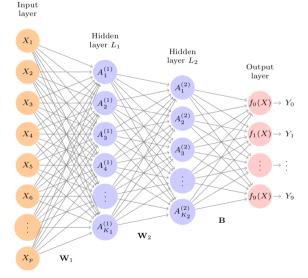
### Neural network architecture for MNIST

- Two hidden layers.
- Softmax for classification output
- We used L<sub>1</sub> has 128 units; L<sub>2</sub> has 64
- 10 output variables due to class labeling
- Result is we are training approx 110K weights

Test your understanding: PollEv

## MNIST learning





0.2 0.4 0.6 0.8 1.0

0

Class Probability

### Section 2

### Convolutional Neural Network

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## Last time: Flattening the image

$$\begin{pmatrix} 1 & 1 & 0 \\ 4 & 2 & 1 \\ 0 & 2 & 1 \end{pmatrix} \longrightarrow \begin{pmatrix} 1 \\ 1 \\ 0 \\ 4 \\ 2 \\ 1 \\ 0 \\ 2 \\ 1 \end{pmatrix}$$

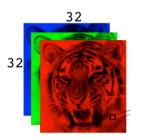
### Example data set: CIFAR100 Data



- 60,000 images: 50K training, 10K test
- Labels with 20 super classes (e.g. aquatic mammals)
- 5 classes per super class (beaver, dolphin, otter, seal, whale)
- Images are 32x32

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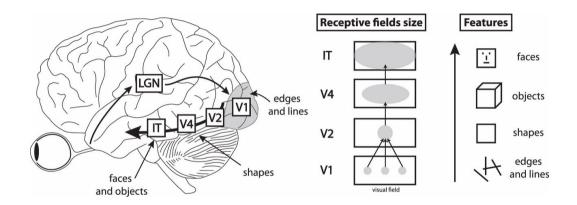
# Image channel data



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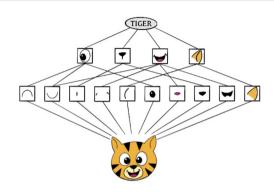
## How does your brain do it? The visual hierarchy



Mauro Manassi, Bilge Sayim, Michael H. Herzog; When crowding of crowding leads to uncrowding. Journal of Vision 2013;13(13):10. https://doi.org/10.1167/13.13.10.

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### **CNNs**



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### Convolution layer

#### Convolution Filter

#### Original Image:

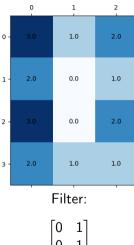
#### Convolution filter:

$$\begin{bmatrix} \alpha & \beta \\ \gamma & \delta \end{bmatrix}$$

#### Convolved Image

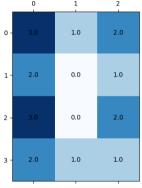
$$\begin{bmatrix} a\alpha + b\beta + d\gamma + e\delta & b\alpha + c\beta + e\gamma + f\delta \\ d\alpha + e\beta + g\gamma + h\delta & e\alpha + f\beta + h\gamma + i\delta \\ g\alpha + h\beta + j\gamma + k\delta & h\alpha + i\beta + k\gamma + l\delta \end{bmatrix}$$

## Convolution Filter Example



## Same example, different filter

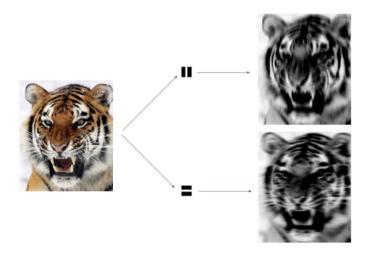
### What is the convolved image?



Filter:

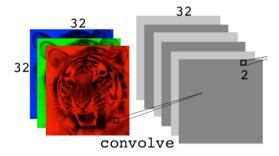
$$\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$$

## Convolution filter: Bigger example



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## Convolution layer



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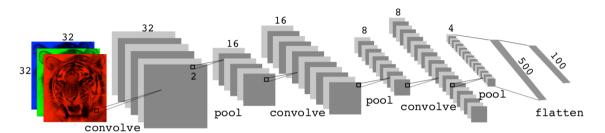
### More notes on convolution

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## Pooling layers

Max pool 
$$\begin{bmatrix} 1 & 2 & 5 & 3 \\ 3 & 0 & 1 & 2 \\ 2 & 1 & 3 & 4 \\ 1 & 1 & 2 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 3 & 5 \\ 2 & 4 \end{bmatrix}$$

### Putting it together to make a CNN



https://poloclub.github.io/cnn-explainer/

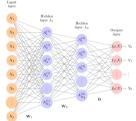
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# Coding

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## TL;DR

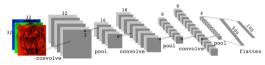
#### Feed Forward Neural Net



$$A_k = h_k(X) = g(w_{k0} + \sum_{j=1}^p w_{kj}X_j),$$

- Combines input data using learned weights
- Linear combo of those to get output
- Sometimes softmax to get probability of classification

#### **CNN**



- Specialized NN
- Gets next layer via
  - Convolution layer
  - Pooling Layer
  - Fully connected layer

### Next time

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Q of the Day: which layer(s) in CNN are more similar in dimension as its previous layer?

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