## Ch 2.1: What is Statistical Learning? Lecture 2 - CMSE 381

#### Prof. Mengsen Zhang

Michigan State University :: Dept of Computational Mathematics, Science & Engineering

Weds, Jan 15, 2025

#### Announcements

#### Last time:

- Discussed where to find everything
  - Course webpage
  - Slack
  - D2L
- Python Refresh!
- Check out the syllabus!

CMSE381\_S2025\_Schedule : Sheet1

Lec #	Date		Торіс	Reading	нพ	
1	М	1/13	Intro / Python Review	1		
2	W	1/15	What is statistical learning	2.1		
3	F	1/17	Assessing Model Accuracy	2.2.1, 2.2.2		
	М	1/20	MLK - No Class			
4	W	1/22	Linear Regression	3.1		
5	F	1/24	More Linear Regression	3.1	HW #1 Due	
6	М	1/27	Multi-linear Regression	3.2	Sun 1/26	
7	w	1/29	Probably More Linear Regression	3.3		

#### **Announcements:**

- Get on slack!
  - +1 point on the first homework if you post a gif in the thread
- First homework due Sun Jan 26th
- First office hours next week

- Input/output variables
- Prediction vs inference
- Reduceable vs irreduceable error
- Overfitting
- Classification vs regression
- Supervised vs Unsupervised learning

• Please note: no jupyter notebook for today's class, slides only

## An example data set: Advertising

	тν	Radio	Newspaper	Sales
	230.1	37.8	69.2	22.1
2	44.5	39.3	45.1	10.4
	17.2	45.9	69.3	9.3
	151.5	41.3	58.5	18.5
5	180.8	10.8	58.4	12.9
6	8.7	48.9	75	7.2
	57.5	32.8	23.5	11.8
8	120.2	19.6	11.6	13.2
9	8.6	2.1		4.8
10	199.8	2.6	21.2	10.6
11	66.1	5.8	24.2	8.6

- Sales of a product in 200 markets, along with amount spent on three differnt types of advertising
- Goal:
- Input variables:
- Output variable:

Data available at msu-cmse-courses.github.io/CMSE381-S25/DataSets/DataSets.html

### Notation and Big Assumption

Input variables:  $X_1, X_2, \cdots, X_p$ Output variable: Y



#### Advertising Example



## More examples





## Section 1

### Prediction vs Inference

Given a value X, try to provide an estimate for f(X).

Build a model:

$$\hat{Y} = \hat{f}(X)$$

Example: If we spend \$250 on TV advertising, what do we predict we will we make in sales?



## Group question:



The blue solid line is f. The green dashed line is  $\hat{f}$ .

- What is the predicted sales for the first three data points using the green dashed line  $\hat{f}$  shown in the graph?
- Using the dashed green line as the predicted model  $\hat{f}$ , what is the error in each of the three predicions?

### Reduceable vs irreducable error

All models are wrong, some are useful.

$$Y - \hat{Y}$$

#### **Reducible Error**

**Irreducible Error** 

#### More on error

- Given estimate  $\hat{f}$  (fixed)
- Set of predictors X (fixed)
- Prediction  $\hat{Y} = \hat{f}(X)$

 $E(Y - \hat{Y})^2 =$ 

#### Inference

Want *f*, but not for prediction (or possibly combined with prediction)

• Which predictors are associated with the response?

• What is the relationship between the response and each predictor?

• Can the relationship between Y and each predictor be adequately summarized using a linear equation? Is it more complicated?

Determine whether each scenario is prediction, inference, or both.

Application	Prediction	Inference
Predict effectiveness of vaccine		
Determine the address written on		
the image of an envelope.		
Identify risk factors for getting long covid.		
Transcribe an audio file of a person talking.		
Predict stock prices.		

## Section 2

## How to estimate *f*?

- *n* data points observed
- $x_{ij}$  is the *j*th predictor for observation *i*
- *y<sub>i</sub>* is the response variable for the *i*th observation
- Training data:

• {
$$(x_1, y_1), (x_2, y_2), \cdots, (x_n, y_n)$$
  
•  $x_i = (x_i, x_{i2}, \cdots, x_{ip})^T$ 

	тν	Radio	Newspaper	Sales
	230.1	37.8	69.2	22.1
2	44.5	39.3	45.1	10.4
3	17.2	45.9	69.3	9.3
4	151.5	41.3	58.5	18.5
5	180.8	10.8	58.4	12.9
6	8.7	48.9	75	7.2
	57.5	32.8	23.5	11.8
8	120.2	19.6	11.6	13.2
9	8.6	2.1		4.8
10	199.8	2.6	21.2	10.6
11	66.1	5.8	24.2	8.6

Step 1: Select a model

Example:

$$f(X) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_p X_p$$

Step 2: Train the model

Example: Find  $\beta'_i s$  so that

 $Y \approx \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_p X_p$ 



### How do you decide on the coefficients?



 $Y \approx \beta_0 + \beta_1 X_1$ 

#### Desmos toy: https://www.desmos.com/calculator/skvt8c7317

#### Example Non-parametric method: Nearest Neighbors

 $N_k(x) =$  Set of k nearest neighbors of x

$$\hat{f}(x) = rac{1}{k} \sum_{x_i \in N_k(x)} y_i$$



#### Parametric methods: Pros and Cons

Pros

Cons

# Overfitting





## Prediction Accuracy vs Model Interpretability



#### Supervised learning:

Training data has response variable y for every input x



#### **Unsupervised Learning:**

Training data does not have response variable y for every input x



## Regression vs Classification

#### Types of variables:

• Quantitative

• Qualitative / Categorical

# Section 3

# Group work

(a) We collect a set of data on the top 500 firms in the US. For each firm we record profit, number of employees, industry and the CEO salary. We are interested in understanding which factors affect CEO salary.

- Is this classification or regression?
- Do we want inference or prediction?
- What is *n*, the number of data points?
- What is *p*, the number of variables?

(b) We are considering launching a new product and wish to know whether it will be a success or a failure. We collect data on 20 similar products that were previously launched. For each product we have recorded whether it was a success or failure, price charged for the product, marketing budget, competition price, and ten other variables.

- Is this classification or regression?
- Do we want inference or prediction?
- What is *n*, the number of data points?
- What is *p*, the number of variables?

Lec 2

# TL;DR

## Wrap up

#### Next time:

- Friday 1/17
- Bring Laptop!
- Monday 1/20
  - MLK, NO CLASS!
- Next week
  - ▶ First homework due Sun 1/26
  - There will be a quiz next week

CMSE381\_S2025\_Schedule : Sheet1

Lec #	Date		Date Topic		нพ	
1	Μ	1/13	Intro / Python Review	1		
2	W	1/15	What is statistical learning	2.1		
3	F	1/17	Assessing Model Accuracy	2.2.1, 2.2.2		
	М	1/20	MLK - No Class			
4	W	1/22	Linear Regression	3.1		
5	F	1/24	More Linear Regression	3.1	HW #1 Due	
6	М	1/27	Multi-linear Regression	3.2	Sun 1/26	
7	w	1/29	Probably More Linear	3.3		

#### **Announcements:**

- Get on slack!
  - +1 point on the first homework if you post a gif in the thread
- Office hours!
  - Dr. Zhang: MW 10-11am
  - Omeiza Olumoye: TTh 3-4 pm