### Ch 10.3: Convolutional Neural Nets

Lecture 31 - CMSE 381

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Fri, Nov 22, 2024

### Announcements

#### Last time:

- Multilayer NN
- pyTorch

#### This lecture:

CNNs

#### **Announcements:**

- Project due Friday
- HW #9 is posted
- Exam 3 is Dec 4th
- Project is due Dec 6th

Lec #	Date			Reading	HW	
21	Mon	10/28	Polynomial & Step Functions	7.1,7.2		
22	Wed	10/30	Step Functions; Basis functions; Start Splines	7.2 - 7.4		
23	Fri	11/1	Regression Splines	7.4	HW #6 Due Sun 11/3	
24	Mon	11/4	Decision Trees	8.1		
25	Wed	11/6	Class Cancelled (Dr Munch	out of town)		
26	Fri	11/8	Random Forests	8.2.1, 8.2.2	HW #7 Due Sun 11/10	
27	Mon	11/11	Maximal Margin Classifier	9.1		
28	Wed	11/13	SVC	9.2		
29	Fri	11/15	SVM	9.3, 9.4	HW #8 Due Sun 11/17	
30	Mon	11/18	Single layer NN	10.1		
31	Wed	11/20	Multi Layer NN	10.2		
32	Fri	11/22	CNN	10.3	HW #11	
33	Mon	11/25	TBD: Unsupervised learning/clustering	12.1, 12.4?	Due Sun 11/24	
	Wed	11/27	Virtual: Project office hours			
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	Mon	12/2	Review			
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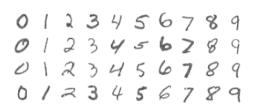
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### Section 1

Last time: Neural Nets

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## **MNIST**



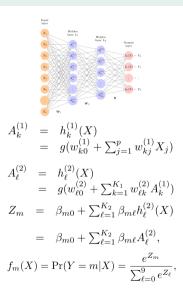






- Goal: Build a model to classify images into their correct digit class
- Each image has  $p = 28 \cdot 28 = 784$  pixels
- Each pixel is grayscale value in [0,255]
- Data converted into column order
- Output represented by one-hot vector  $Y = (Y_0, Y_1, \cdots, Y_9)$
- 60K training images, 10K test images

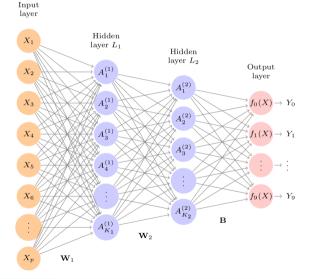
### Neural network architecture for MNIST

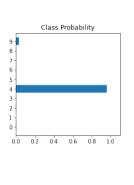


- Two hidden layers.
- Softmax for classification output
- We used  $L_1$  has 128 units;  $L_2$  has 64
- 10 output variables due to class labeling
- Result is we are training approx 110K weights

# MNIST learning







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### Section 2

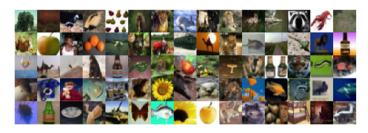
### Convolutional Neural Network

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Last time: Flattening the image

$$\begin{pmatrix} 1 & 1 & 0 \\ 4 & 2 & 1 \\ 0 & 2 & 1 \end{pmatrix} \longrightarrow \begin{pmatrix} 1 \\ 1 \\ 0 \\ 4 \\ 2 \\ 1 \\ 0 \\ 2 \\ 1 \end{pmatrix}$$

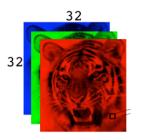
## Example data set: CIFAR100 Data



- 60,000 images: 50K training, 10K test
- Labels with 20 super classes (e.g. aquatic mammals)
- 5 classes per super class (beaver, dolphin, otter, seal, whale)
- Images are 32x32

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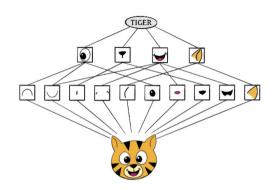
# Image channel data



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## **CNNs**



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# Convolution layer

#### Convolution Filter

### Original Image:

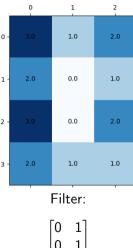
### Convolution filter:

$$\begin{bmatrix} \alpha & \beta \\ \gamma & \delta \end{bmatrix}$$

### Convolved Image

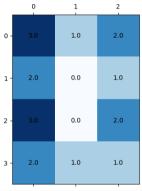
$$\begin{bmatrix} a\alpha + b\beta + d\gamma + e\delta & b\alpha + c\beta + e\gamma + f\delta \\ d\alpha + e\beta + g\gamma + h\delta & e\alpha + f\beta + h\gamma + i\delta \\ g\alpha + h\beta + j\gamma + k\delta & h\alpha + i\beta + k\gamma + l\delta \end{bmatrix}$$

# Convolution Filter Example



# Same example, different filter

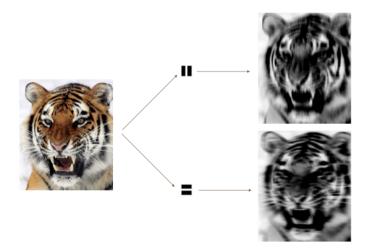
What is the convolved image?



Filter:

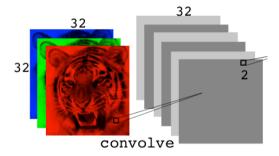
 $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$ 

# Convolution filter: Bigger example



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# Convolution layer



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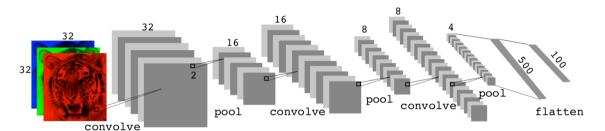


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# Pooling layers

Max pool 
$$\begin{bmatrix} 1 & 2 & 5 & 3 \\ 3 & 0 & 1 & 2 \\ 2 & 1 & 3 & 4 \\ 1 & 1 & 2 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 3 & 5 \\ 2 & 4 \end{bmatrix}$$

## Putting it together to make a CNN



https://poloclub.github.io/cnn-explainer/

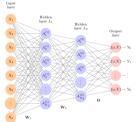
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# Coding

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# TL;DR

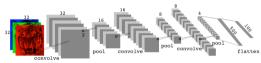
#### **Feed Forward Neural Net**



$$A_k = h_k(X) = g(w_{k0} + \sum_{j=1}^p w_{kj}X_j),$$

- Combines input data using learned weights
- Linear combo of those to get output
- Sometimes softmax to get probability of classification

### **CNN**



- Specialized NN
- Gets next layer via
  - Convolution layer
  - Pooling Layer
  - Fully connected layer

## Next time

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